

Parallels between momentum and energy (algebra-based physics)

| Impulse and momentum | Work and energy |
|--|---|
| $\vec{p} := m\vec{v}$ | $KE := \frac{1}{2}mv^2$ |
| $\Delta\vec{J}_F := \vec{F}_{AVG} \Delta t$ $\Delta J_{F,x} = F_{x,AVG} \Delta t$ $\Delta J_{F,y} = F_{y,AVG} \Delta t$ $\Delta J_{F,x,y} = \text{Signed area under graph of } F_{x,y} \text{ vs. } t$ | $\Delta W_F := F_{\parallel,AVG} \Delta \ell$ $= (F \cos \theta)_{AVG} \Delta \ell$ $\Delta W_F = \text{Signed area under graph of } F_{\parallel} \text{ vs. } \ell$ $[W] = \text{N} \cdot \text{m} = \text{J}$ |
| $\vec{p}_i + \sum_F \overbrace{\Delta\vec{J}_F}^{\Delta\vec{J}_{\Sigma F}} = \vec{p}_f$ | $KE_i + \sum_F \overbrace{\Delta W_F}^{\Delta W_{\Sigma F}} = KE_f$ |
| $\vec{F}_{AVG} = \frac{\Delta\vec{J}_F}{\Delta t} = \frac{\Delta\vec{p}_F}{\Delta t}$ | $P_{F,AVG} := \frac{\Delta W_F}{\Delta t}$ $P_F = (F \cos \theta)v$ $[P] = \frac{\text{J}}{\text{s}} = \text{W}$ |
| | $-\Delta U_{F,1\dots N} := \Delta W_{F,2 \text{ ON } 1} + \Delta W_{F,1 \text{ ON } 2} + \dots + \Delta W_{F,N-1 \text{ ON } N}$ $F_{x,AVG} = -\frac{\Delta U_F}{\Delta x}$ $\Delta U_G = mg\Delta h$ $\Delta U_S = \frac{1}{2}k(\Delta x)^2$ |
| $\Sigma \vec{p}_i + \sum_{\substack{\text{EXT} \\ \text{ON SYS}}} \overbrace{\Delta\vec{J}_F}^{\Delta\vec{J}_{\Sigma F, \text{EXT ON SYS}}} = \Sigma \vec{p}_f$ | $\overbrace{\Sigma KE_i + \Sigma U_{G,i} + \Sigma U_{S,i}}^{\Sigma ME_{\text{SYS},i}} + \Sigma \Delta W_{\text{OUF}} = \overbrace{\Sigma KE_f + \Sigma U_{G,f} + \Sigma U_{S,f}}^{\Sigma ME_{\text{SYS},f}} + \Sigma \Delta U_{\text{INT}}$ |